

Package ‘mpmsim’

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Title Simulation of Matrix Population Models with Defined Life History Characteristics

Version 1.1.0

Description Allows users to simulate matrix population models with particular characteristics based on aspects of life history such as mortality trajectories and fertility trajectories. Also allows the exploration of sampling error due to small sample size.

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URL <https://github.com/jonesor/mpmsim>

BugReports <https://github.com/jonesor/mpmsim/issues>

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add_mpm_error	<i>Add sampling error to matrix population models (MPMs) based on expected values of transition rates and sample sizes</i>
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Description

Produces a list of matrix population models based on expected values in the transition matrix and sample size. The expected values are provided in lists of two submatrices: `mat_U` for the growth/development and survival transitions and `mat_F` for the fecundity transitions. The output `mat_U` values are simulated based on expected probabilities, assuming a binomial process with a sample size defined by `sample_size`. The output `mat_F` values are simulated using a Poisson process with a sample size defined by `sample_size`. Thus users can expect that large sample sizes will result in simulated matrices that match closely with the expectations, while simulated matrices with small sample sizes will be more variable.

Usage

```
add_mpm_error(mat_U, mat_F, sample_size, split = TRUE, by_type = TRUE)
```

Arguments

<code>mat_U</code>	A list of U submatrices, or a single U submatrix.
<code>mat_F</code>	A list of F submatrices, or a single F submatrix.
<code>sample_size</code>	either (1) a single matrix of sample sizes for each element of every MPM, (2) a list of two named matrices (" <code>mat_F_ss</code> ", " <code>mat_U_ss</code> ") containing sample sizes for the survival and fertility submatrices of every MPM or (3) a single value applied to the every element of every matrix.
<code>split</code>	logical, whether to split the output into survival and fecundity matrices or not. Defaults to TRUE.
<code>by_type</code>	A logical indicating whether the matrices should be returned in a list by type (A, U, F, C). If <code>split</code> is FALSE, then <code>by_type</code> must also be FALSE. Defaults to TRUE.

Details

if any `sample_size` input is 0, it is assumed that the estimate for the element(s) concerned is known without error.

Value

list of matrices of survival and fecundity if `split = TRUE`, otherwise a single matrix of the sum of survival and fecundity.

Author(s)

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See Also

Other errors: [calculate_errors\(\)](#), [compute_ci\(\)](#)

Other errors: [calculate_errors\(\)](#), [compute_ci\(\)](#)

Examples

```
set.seed(42) # set seed for repeatability

# First generate a set of MPMS
mpm_set <- generate_mpm_set(n = 5, n_stages = 5, fecundity = c(
  0, 0, 4, 8, 10
), archetype = 4, split = TRUE, by_type = TRUE, as_compadre = FALSE)

# Now apply sampling error to this set
add_mpm_error(
  mat_U = mpm_set$U_list, mat_F = mpm_set$F_list, sample_size =
  50
)

# Also works with a single matrix.
mats <- make_leslie_mpm(
  survival = c(0.1, 0.2, 0.5),
  fertility = c(0, 1.2, 2.4),
  n_stages = 3, split = TRUE
)

# Sample size is a single value
add_mpm_error(mat_U = mats$mat_U, mat_F = mats$mat_F, sample_size = 20)

# Sample size is a list of two matrices
# here with a sample size of 20 for reproduction and 10 for growth/survival.
mpm_set <- generate_mpm_set(
  n = 5, n_stages = 3, fecundity = c(0, 2, 4),
  archetype = 4, split = TRUE, by_type = TRUE,
  as_compadre = FALSE
)

ssMats <- list(
  "mat_F_ss" = matrix(20, nrow = 3, ncol = 3),
  "mat_U_ss" = matrix(10, nrow = 3, ncol = 3)
)
```

```
# Add sampling error to the matrix models
output <- add_mpm_error(
  mat_U = mpm_set$U_list, mat_F = mpm_set$F_list,
  sample_size = ssMats
)

# Examine the outputs
names(output)
output
```

calculate_errors	<i>Calculate error (standard error or 95%CI) in elements of a matrix population model.</i>
------------------	--

Description

Given two submatrices of a matrix population model (`mat_U` and `mat_F`, the growth/survival matrix and the reproduction matrix respectively) and a sample size, or matrix/matrices of sample sizes, this function calculates the standard error or 95% confidence interval (95%CI) for each element of the matrix. These calculations assume that `mat_U` is the result of binomial processes (i.e., the survival (0/1) of a sample of n individuals), while `mat_F` is the result of Poisson processes (i.e., counts of offspring from n individuals), where n is the sample size.

Usage

```
calculate_errors(mat_U, mat_F, sample_size, type = "sem", calculate_A = TRUE)
```

Arguments

<code>mat_U</code>	matrix of mean survival probabilities
<code>mat_F</code>	matrix of mean fecundity values
<code>sample_size</code>	either (1) a single matrix of sample sizes for each element of the MPM, (2) a list of two named matrices (" <code>mat_F_ss</code> ", " <code>mat_U_ss</code> ") containing sample sizes for the survival and fertility submatrices of the MPM or (3) a single value applied to the whole matrix
<code>type</code>	A character string indicating the type of error to calculate. Must be one of "sem" (standard error), or "CI95" (95% confidence interval).
<code>calculate_A</code>	A logical argument indicating whether the returned error information should include the A matrix and its error. Defaults to TRUE.

Details

The output is a list containing the original matrices and matrices showing error estimates or confidence intervals.

Value

A list containing the original matrices and the error estimates (or upper and lower confidence intervals) for the U, F and (optionally) A matrices.

Author(s)

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See Also

[add_mpm_error\(\)](#) which simulates matrices with known values and sample sizes.

Other errors: [add_mpm_error\(\)](#), [compute_ci\(\)](#)

Examples

```
# Set up two submatrices
matU <- matrix(c(
  0.1, 0,
  0.2, 0.4
), byrow = TRUE, nrow = 2)
matF <- matrix(c(
  0, 4,
  0., 0.
), byrow = TRUE, nrow = 2)

# errors as 95% CI, with a sample size of 20 for all elements
calculate_errors(mat_U = matU, mat_F = matF, sample_size = 20, type = "CI95")

# errors as sem, with a sample size of 20 for all elements
calculate_errors(mat_U = matU, mat_F = matF, sample_size = 20, type = "sem")

# Sample size is a single matrix applied to both F and U matrices
ssMat <- matrix(10, nrow = 2, ncol = 2)

calculate_errors(
  mat_U = matU, mat_F = matF, sample_size = ssMat, type =
    "sem"
)

# Sample size is a list of two matrices, one for F and one for U.
ssMats <- list(
  "mat_F_ss" = matrix(10, nrow = 2, ncol = 2),
  "mat_U_ss" = matrix(10, nrow = 2, ncol = 2)
)
calculate_errors(
  mat_U = matU, mat_F = matF, sample_size = ssMats, type =
    "sem"
)
```

compute_ci	<i>Compute 95% confidence intervals for derived estimates from a matrix population model</i>
------------	--

Description

This function computes the 95% confidence interval for measures derived from a matrix population model using parametric bootstrapping. In this approach a sampling distribution of the matrix population model (MPM) is generated by taking a large number of random independent draws using the sampling distribution of each underlying transition rate. The approach rests on our assumption that survival-related processes are binomial, while reproduction is a Poisson process (see the function `add_mpm_error()` for details).

Usage

```
compute_ci(mat_U, mat_F, sample_size, FUN, ..., n_sim = 1000, dist.out = FALSE)
```

Arguments

mat_U	A matrix that describes the growth and survival process.
mat_F	A matrix that describes reproduction.
sample_size	either (1) a single matrix of sample sizes for each element of the MPM, (2) a list of two named matrices ("mat_F_ss", "mat_U_ss") containing sample sizes for the survival and fertility submatrices of the MPM or (3) a single value applied to the whole matrix
FUN	A function to apply to each simulated matrix population model. This function must take, as input, a single matrix population model (i.e., the A matrix).
...	Additional arguments to be passed to FUN.
n_sim	An integer indicating the number of simulations to run. Default is 1000.
dist.out	Logical. If TRUE, returns a list with both the quantiles and the simulated estimates. Default is FALSE.

Details

The inputs are the U matrix, which describes the survival-related processes, and the F matrix which describes reproduction. The underlying assumption is that the U matrix is the average of a binomial process while the F matrix is the average of a Poisson process. The confidence interval will depend largely on the sample size used.

Value

If `dist.out` is FALSE, a numeric vector of the 2.5th and 97.5th quantiles of the estimated measures. If `dist.out = TRUE`, a list with two elements: `quantiles` is a numeric vector of the 2.5th and 97.5th quantiles of the estimated measures, and `estimates` is a numeric vector of the estimated measures.

Author(s)

Owen Jones jones@biology.sdu.dk

References

Chapter 12 in Caswell, H. (2001). *Matrix Population Models*. Sinauer Associates Incorporated.

See Also

Other errors: [add_mpm_error\(\)](#), [calculate_errors\(\)](#)

Examples

```
set.seed(42) # set seed for repeatability

# Data for use in example
matU <- matrix(c(
  0.1, 0.0,
  0.2, 0.4
), byrow = TRUE, nrow = 2)

matF <- matrix(c(
  0.0, 5.0,
  0.0, 0.0
), byrow = TRUE, nrow = 2)

set.seed(42)

# Example of use to calculate 95% CI of lambda
compute_ci(
  mat_U = matU, mat_F = matF, sample_size = 10, FUN =
  popbio::lambda
)

# Example of use to calculate 95% CI of generation time
compute_ci(
  mat_U = matU, mat_F = matF, sample_size = 40, FUN =
  popbio::generation.time
)

# Example of use to calculate 95% CI of generation time and show the
# distribution of those bootstrapped estimates
xx <- compute_ci(
  mat_U = matU, mat_F = matF, sample_size = 100, FUN =
  popbio::generation.time, dist.out = TRUE
)
summary(xx$quantiles)
hist(xx$estimates)
```

driven_vital_rate *Calculate driven vital rates*

Description

This function calculates new values for a vital rate, such as survival or fecundity that is being influenced by a driver (e.g., weather). It does this by using a driver variable and a baseline value, along with a specified slope for the relationship between the driver variable and the vital rate. The function works on a linearised scale, using logit for survival and log for fecundity, and takes into account the error standard deviation.

Usage

```
driven_vital_rate(
  driver,
  baseline_value = NULL,
  slope = NULL,
  baseline_driver = NULL,
  error_sd = 0,
  link = "logit"
)
```

Arguments

driver	A vector of driver values.
baseline_value	A vector or matrix of baseline values for the vital rate (e.g., survival) that is being influenced ("driven") by another variable (e.g. a climatic variable).
slope	A vector or matrix of slopes for the relationship between the driver variable and the vital rate being driven.
baseline_driver	The baseline_driver parameter is a single value representing the baseline driver value. If the driver value is greater than this value and the slope is positive, then the resulting vital rate will be higher. Conversely, if the driver value is less than this variable and the slope is positive, then the resulting vital rate will be less than the baseline value.
error_sd	A vector or matrix of error standard deviations for random normal error to be added to the driven value of the vital rate being modelled. If set to 0 (the default), no error is added.
link	A character string indicating the type of link function to use. Valid values are "logit" (the default) and "log", which are appropriate for survival (U submatrix) and reproduction (F submatrix) respectively.

Details

The relationship between the driver variable and the vital rate is assumed to be linear:

$$V = a * (d - d_b) + x + E$$

Where V is the new vital rate (on the scale of the linear predictor), a is the slope, x is the baseline vital rate, d is the driver, d_b is the baseline driver and E is the error.

The input vital rate(s) (`baseline_value`) can be a single-element vector representing a single vital rate (e.g., survival probability or fecundity), a longer vector representing a series of vital rates (e.g., several survival probabilities or fecundity values), or a matrix of values (e.g., a U or F submatrix of a matrix population model). The slopes of the relationship between the vital rate (`baseline_value`) and the driver can be provided as a single value, which is applied to all elements of the input vital rates, or as a matrix of values that map onto the matrix of vital rates. This allows users to simulate cases where different vital rates in a matrix model are affected in different ways by the same weather driver. For example, juvenile survival might be more affected by the driver than adult survival. The `baseline_driver` value represents the "normal" state of the driver. If the driver is greater than the `baseline_driver` and the slope is positive, then the outcome vital rate will be higher. If the driver is less than the `baseline_driver` variable and the slope is positive, then the outcome vital rate will be less than the `baseline_value`. The `error_sd` represents the error in the linear relationship between the driver and the vital rate.

Value

Depending on the input types, either a single value, a vector or a list of matrices of driven values for the vital rate(s) being modelled. The list has a length equal to the length of the driver input parameter.

Author(s)

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Examples

```
set.seed(42) # set seed for repeatability

# A single vital rate and a single driver
driven_vital_rate(
  driver = 14,
  baseline_value = 0.5,
  slope = .4,
  baseline_driver = 10,
  error_sd = 0,
  link = "logit"
)

# A single vital rate and a time series of drivers
driven_vital_rate(
  driver = runif(10, 5, 15),
  baseline_value = 0.5,
  slope = .4,
  baseline_driver = 10,
  error_sd = 0,
  link = "logit"
)

# A matrix of survival values (U submatrix of a Leslie model)
```

```

# with a series of drivers, and matrices of slopes and errors

lt1 <- model_survival(params = c(b_0 = 0.4, b_1 = 0.5), model = "Gompertz")
lt1$fert <- model_fertility(
  age = 0:max(lt1$x), params = c(A = 10),
  maturity = 3, model = "step"
)

mats <- make_leslie_mpm(
  survival = lt1$px, fertility = lt1$fert, n_stages =
  nrow(lt1), split = TRUE
)
mats$mat_U
mat_dim <- nrow(mats$mat_U)

driven_vital_rate(
  driver = runif(5, 5, 15),
  baseline_value = mats$mat_U,
  slope = matrix(.4,
    nrow = mat_dim,
    ncol = mat_dim
  ),
  baseline_driver = 10,
  error_sd = matrix(1, nrow = mat_dim, ncol = mat_dim),
  link = "logit"
)

```

generate_mpm_set

Generate lists of Lefkovich matrix population models (MPMs) based on life history archetypes

Description

This function generates a list of n MPMs according to the specified criteria. Criteria include the archetype, and the acceptable constraining criteria, which could include lambda, generation time or any other metric derived from an A matrix. The function attempts to find matrices that fulfil the criteria, discarding unacceptable matrices. By default, if it takes more than 1000 attempts to find a suitable matrix model, then an error is produced. However, the number of attempts can be altered with the attempts parameter.

Usage

```

generate_mpm_set(
  n = 10,
  n_stages = 3,
  archetype = 1,
  fecundity = 1.5,
  split = TRUE,

```

```

    by_type = TRUE,
    as_compadre = TRUE,
    max_surv = 0.99,
    constraint = NULL,
    attempts = 1000
  )

```

Arguments

n	The number of MPMs to generate. Default is 10.
n_stages	The number of stages for the MPMs. Default is 3.
archetype	The archetype of the MPMs. Default is 1.
fecundity	A vector of fecundities for the MPMs. Default is 1.5.
split	A logical indicating whether to split into submatrices. Default is TRUE.
by_type	A logical indicating whether the matrices should be returned in a list by type (A, U, F, C). If split is FALSE, then by_type must also be FALSE. Defaults to TRUE.
as_compadre	A logical indicating whether the matrices should be returned as a CompadreDB object. Default is TRUE. This requires argument by_type to be TRUE. If FALSE, the function returns a list.
max_surv	The maximum acceptable survival value. Defaults to 0.99. This is only used if split = TRUE.
constraint	An optional data frame with 4 columns named fun, arg, lower and upper. These columns specify (1) a function that outputs a metric derived from an A matrix and (2) an argument for the function (NA, if no argument supplied) (3) the lower acceptable bound for the metric and (4) upper acceptable bound for the metric. This could be used to specify
attempts	An integer indicating the number of attempts To be made when simulating matrix model. The default is 1000. If it takes more than 1000 attempts to make a matrix that satisfies the conditions set by the other arguments, then a warning is produced.

Value

A list of MPMs that meet the specified criteria.

Author(s)

Owen Jones jones@biology.sdu.dk

See Also

[random_mpm\(\)](#) which this function is essentially a wrapper for.

Other Lefkovitch matrices: [random_mpm\(\)](#)

Examples

```

set.seed(42) # set seed for repeatability

# Basic operation, without splitting matrices and with no constraints
generate_mpm_set(
  n = 10, n_stages = 5, fecundity = c(0, 0, 4, 8, 10),
  archetype = 4, split = FALSE, by_type = FALSE, as_compadre = FALSE
)

# Constrain outputs to A matrices with lambda between 0.9 and 1.1
library(popbio)
constrain_df <- data.frame(
  fun = "lambda", arg = NA, lower = 0.9, upper =
    1.1
)
)
generate_mpm_set(
  n = 10, n_stages = 5, fecundity = c(0, 0, 4, 8, 10),
  archetype = 4, constraint = constrain_df, as_compadre = FALSE
)

# As above, but using popdemo::eigs function instead of popbio::lambda
# to illustrate use of argument
library(popdemo)
constrain_df <- data.frame(
  fun = "eigs", arg = "lambda", lower = 0.9, upper =
    1.1
)
)
generate_mpm_set(
  n = 10, n_stages = 5, fecundity = c(0, 0, 4, 8, 10),
  archetype = 4, constraint = constrain_df, as_compadre = FALSE
)

# Multiple constraints
# Constrain outputs to A matrices with lambda between 0.9 and 1.1, generation
# time between 3 and 5 and damping ratio between 1 and 7.
library(popbio)
constrain_df <- data.frame(
  fun = c("lambda", "generation.time", "damping.ratio"),
  arg = c(NA, NA, NA),
  lower = c(0.9, 3.0, 1.0),
  upper = c(1.1, 5.0, 7.0)
)
)
generate_mpm_set(
  n = 10, n_stages = 5, fecundity = c(0, 0, 4, 8, 10),
  archetype = 4, constraint = constrain_df, as_compadre = FALSE
)
)

```

Description

The function creates a Leslie matrix from inputs of number of stages, fertility (the top row of the matrix), and survival probability (the value in the sub-diagonal).

Usage

```
make_leslie_mpm(survival, fertility, n_stages, split = FALSE)
```

Arguments

survival	a numeric value representing the survival probability of each stage along the lower off-diagonal of the matrix, with the final value being in the lower-right corner of the matrix. If only one value is provided, this is applied to all survival elements.
fertility	a numeric vector of length <code>n_stages</code> representing the fertility rate of each stage. If only one value is provided, this is applied to all fertility elements.
n_stages	a numeric value representing the number of stages in the matrix
split	a logical argument indicating whether the output matrix should be split into separate A, U and F matrices (where $A = U + F$).

Value

A matrix of size `n_stages` x `n_stages` representing the Leslie matrix

Author(s)

Owen Jones jones@biology.sdu.dk

References

- Caswell, H. (2001). Matrix Population Models: Construction, Analysis, and Interpretation. Sinauer.
- Leslie, P. H. (1945). On the use of matrices in certain population mathematics. *Biometrika*, 33 (3), 183–212.
- Leslie, P. H. (1948). Some Further Notes on the Use of Matrices in Population Mathematics. *Biometrika*, 35(3-4), 213–245.

See Also

- [model_survival\(\)](#) to model age-specific survival using mortality models.
- [model_fertility\(\)](#) to model age-specific fertility using various functions.

Examples

```
make_leslie_mpm(  
  survival = 0.5, fertility = c(0.1, 0.2, 0.3),  
  n_stages = 3, split = FALSE  
)  
make_leslie_mpm(  
  survival = 0.5, fertility = c(0.1, 0.2, 0.3),  
  n_stages = 3, split = FALSE  
)
```

```

    survival = c(0.5, 0.6, 0.7), fertility = c(0.1, 0.2, 0.3),
    n_stages = 3
  )
  make_leslie_mpm(
    survival = seq(0.1, 0.7, length.out = 4), fertility = 0.1,
    n_stages = 4
  )
  make_leslie_mpm(
    survival = c(0.8, 0.3, 0.2, 0.1, 0.05), fertility = 0.2,
    n_stages = 5
  )

```

 model_fertility

Model fertility with age using set functional forms

Description

This function computes fertility based on the logistic, step, von Bertalanffy, Hadwiger, and normal models. The logistic model assumes that fertility increases sigmoidally with age from maturity until a maximum fertility is reached. The step model assumes that fertility is zero before the age of maturity and then remains constant. The von Bertalanffy model assumes that, after maturity, fertility increases asymptotically with age until a maximum fertility is reached. In this formulation, the model is set up so that fertility is 0 at the 'age of maturity - 1', and increases from that point. The Hadwiger model is rather complex and is intended to model human fertility with a characteristic hump-shaped fertility. For all models, the output ensures that fertility is zero before the age at maturity.

Usage

```
model_fertility(params, age = NULL, maturity = 0, model = "logistic")
```

Arguments

params	A numeric vector of parameters for the selected model. The number and meaning of parameters depend on the selected model.
age	A numeric vector representing age.
maturity	A non-negative numeric value indicating the age at maturity. Whatever model is used, the fertility is forced to be 0 below the age of maturity.
model	A character string specifying the model to use. Must be one of "logistic", "step", "vonbertalanffy", "normal" or "hadwiger".

Details

The required parameters varies depending on the fertility model. The parameters are provided as a vector and the parameters must be provided in the order mentioned here.

- Logistic: $f(x) = A/(1 + \exp(-k(x - x_m)))$

- Step: $f(x) = \begin{cases} A, x \geq m \\ A, x < m \end{cases}$
- von Bertalanffy: $f(x) = A(1 - \exp(-k(x - x_0)))$
- Normal: $f(x) = A \times \exp\left(-\frac{1}{2} \left(\frac{x-\mu}{\sigma}\right)^2\right)$
- Hadwiger: $f(x) = \frac{ab}{c} \left(\frac{c}{x}\right)^{\frac{3}{2}} \exp\left\{-b^2 \left(\frac{c}{x} + \frac{x}{c} - 2\right)\right\}$

Value

A numeric vector representing the computed fertility values.

Author(s)

Owen Jones jones@biology.sdu.dk

References

- Bertalanffy, L. von (1938) A quantitative theory of organic growth (inquiries on growth laws. II). *Human Biology* 10:181–213.
- Peristera, P. & Kostaki, A. (2007) Modeling fertility in modern populations. *Demographic Research*. 16. Article 6, 141-194 [doi:10.4054/DemRes.2007.16.6](https://doi.org/10.4054/DemRes.2007.16.6)

See Also

[model_survival\(\)](#) to model age-specific survival using mortality models.

Other trajectories: [model_survival\(\)](#)

Examples

```
# Compute fertility using the step model
model_fertility(age = 0:20, params = c(A = 10), maturity = 2, model = "step")

# Compute fertility using the logistic model
model_fertility(
  age = 0:20, params = c(A = 10, k = 0.5, x_m = 8), maturity =
    0, model = "logistic"
)

# Compute fertility using the von Bertalanffy model
model_fertility(
  age = 0:20, params = c(A = 10, k = .3), maturity = 2, model =
    "vonbertalanffy"
)

# Compute fertility using the normal model
model_fertility(
  age = 0:20, params = c(A = 10, mu = 4, sd = 2), maturity = 0,
  model = "normal"
)
```

```
# Compute fertility using the Hadwiger model
model_fertility(
  age = 0:50, params = c(a = 0.91, b = 3.85, c = 29.78),
  maturity = 0, model = "hadwiger"
)
```

model_survival	<i>Model mortality hazard, survivorship and age-specific survival probability using a mortality model</i>
----------------	---

Description

Model mortality hazard, survivorship and age-specific survival probability using a mortality model

Usage

```
model_survival(params, age = NULL, model, truncate = 0.01)
```

```
model_mortality(params, age = NULL, model, truncate = 0.01)
```

Arguments

params	Numeric vector representing the parameters of the mortality model.
age	Numeric vector representing age. The default is NULL, whereby the survival trajectory is modelled from age 0 to the age at which the survivorship of the synthetic cohort declines to a threshold defined by the truncate argument, which has a default of 0.01 (i.e. 1% of the cohort remaining alive).
model	Mortality model: Gompertz, GompertzMakeham, Exponential, Siler.
truncate	a value defining how the life table output should be truncated. The default is 0.01, indicating that the life table is truncated so that survivorship, l_x , > 0.01 (i.e. the age at which 1% of the cohort remains alive).

Details

The required parameters varies depending on the mortality model. The parameters are provided as a vector. For Gompertz, the parameters are b_0 , b_1 . For GompertzMakeham the parameters are b_0 , b_1 and C . For Exponential, the parameter is C . For Siler, the parameters are a_0 , a_1 , C , b_0 and b_1 . Note that the parameters must be provided in the order mentioned here. x represents age.

- Gompertz: $h_x = b_0 e^{b_1 x}$
- Gompertz-Makeham: $h_x = b_0 e^{b_1 x} + c$
- Exponential: $h_x = c$
- Siler: $h_x = a_0 e^{-a_1 x} + c + b_0 e^{b_1 x}$

In the output, the probability of survival (px) (and death (qx)) represent the probability of individuals that enter the age interval $[x, x + 1]$ survive until the end of the interval (or die before the end of the interval). It is not possible to estimate a value for this in the final row of the life table (because there is no $x + 1$ value) and therefore the input values of age (x) may need to be extended to capture this final interval.

Value

A data frame with columns for age (x), hazard (hx), survivorship (lx) and mortality (qx) and survival probability within interval (px).

Author(s)

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References

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- Pinder III, J.E., Wiener, J.G. & Smith, M.H. (1978) The Weibull distribution: a method of summarizing survivorship data. *Ecology*, 59, 175–179.
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- Siler, W. (1979) A competing-risk model for animal mortality. *Ecology*, 60, 750–757.
- Vaupel, J., Manton, K. & Stallard, E. (1979) The impact of heterogeneity in individual frailty on the dynamics of mortality. *Demography*, 16, 439–454.

See Also

[model_fertility\(\)](#) to model age-specific fertility using various functions.

Other trajectories: [model_fertility\(\)](#)

Examples

```
model_survival(params = c(b_0 = 0.1, b_1 = 0.2), model = "Gompertz")

model_survival(
  params = c(b_0 = 0.1, b_1 = 0.2, C = 0.1),
  model = "GompertzMakeham",
  truncate = 0.1
)

model_survival(params = c(c = 0.2), model = "Exponential", age = 0:10)

model_survival(
  params = c(a_0 = 0.1, a_1 = 0.2, C = 0.1, b_0 = 0.1, b_1 = 0.2),
  model = "Siler",
  age = 0:10
)

model_mortality(params = c(b_0 = 0.1, b_1 = 0.2), model = "Gompertz")
```

plot_matrix	<i>Plot a matrix as a heatmap</i>
-------------	-----------------------------------

Description

Visualise a matrix, such as a matrix population model (MPM), as a heatmap.

Usage

```
plot_matrix(mat, zero_na = FALSE, legend = FALSE, na_colour = NA, ...)
```

Arguments

mat	A matrix, such as the A matrix of a matrix population model
zero_na	Logical indicating whether zero values should be treated as NA
legend	Logical indicating whether to include a legend
na_colour	Colour for NA values
...	Additional arguments to be passed to ggplot

Value

A ggplot object

Author(s)

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Examples

```
matDim <- 10
A1 <- make_leslie_mpm(
  survival = seq(0.1, 0.7, length.out = matDim),
  fertility = seq(0.1, 0.7, length.out = matDim),
  n_stages = matDim
)
plot_matrix(A1, zero_na = TRUE, na_colour = "black")
plot_matrix(A1, zero_na = TRUE, na_colour = NA)
```

random_mpm	<i>Generate random Lefkovich matrix population models (MPMs) based on life history archetypes</i>
------------	---

Description

Generates a random matrix population model (MPM) with element values based on defined life history archetypes. Survival and transition/growth probabilities from any particular stage are restricted to be less than or equal to 1 by drawing from a Dirichlet distribution. The user can specify archetypes (from Takada et al. 2018) to restrict the MPMs in other ways:

- Archetype 1: all elements are positive, although they may be very small. Therefore, transition from/to any stage is possible. This model describes a life history where individuals can progress and retrogress rapidly.
- Archetype 2: has the same form as archetype 1 (transition from/to any stage is possible), but the survival probability (column sums of the survival matrix) increases monotonously as the individuals advance to later stages. This model, as the one in the first archetype, also allows for rapid progression and retrogression, but is more realistic in that stage-specific survival probability increases with stage advancement.
- Archetype 3: positive non-zero elements for survival are only allowed on the diagonal and lower sub-diagonal of the matrix. This model represents the life cycle of a species where retrogression is not allowed, and progression can only happen to the immediately larger/more developed stage (slow progression, e.g., trees).
- Archetype 4: This archetype has the same general form as archetype 3, but with the further assumption that stage-specific survival increases as individuals increase in size/developmental stage. In this respect it is similar to archetype 2.

Usage

```
random_mpm(n_stages, fecundity, archetype = 1, split = FALSE)
```

Arguments

n_stages	An integer defining the number of stages for the MPM.
fecundity	Fecundity is the average number of offspring produced. Values can be provided in 4 ways: <ul style="list-style-type: none"> • An numeric vector of length 1 to provide a fecundity measure to the top right corner of the matrix model only. • A numeric vector of integers of length equal to n_stages to provide fecundity estimates for the whole top row of the matrix model. Use 0 for cases with no reproduction. • A matrix of numeric values of the same dimension as n_stages to provide fecundity estimates for the entire matrix model. Use 0 for cases with no reproduction.

- A list of two matrices of numeric values, both with the same dimension as `n_stages`, to provide lower and upper estimates of mean fecundity for the entire matrix model. In the latter case, a fecundity value will be drawn from a uniform distribution for the defined range. If there is no reproduction in a particular age class, use a value of 0 for both the lower and upper limit.

<code>archetype</code>	Indication of which life history archetype should be used, based on Takada et al. 2018. An integer between 1 and 4.
<code>split</code>	TRUE/FALSE, indicating whether the matrix produced should be split into a survival matrix and a fertility matrix. Yeah true, then the output becomes a list with a matrix in each element. Otherwise, the output is a single matrix.

Details

In all 4 of these Archetypes, fecundity is placed as a single element on the top right of the matrix, if it is a single value. If it is a vector of length `n_stages` then the fertility vector spans the entire top row of the matrix.

The function is constrained to only output ergodic matrices.

Value

Returns a random matrix population model with characteristics determined by the archetype selected and fecundity vector. If `split = TRUE`, the matrix is split into separate fertility and a growth/survival matrices, returned as a list.

Author(s)

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References

- Caswell, H. (2001). *Matrix Population Models: Construction, Analysis, and Interpretation*. Sinauer.
- Lefkovitch, L. P. (1965). The study of population growth in organisms grouped by stages. *Biometrics*, 21(1), 1.
- Takada, T., Kawai, Y., & Salguero-Gómez, R. (2018). A cautionary note on elasticity analyses in a ternary plot using randomly generated population matrices. *Population Ecology*, 60(1), 37–47.

See Also

[generate_mpm_set\(\)](#) which is a wrapper for this function allowing the generation of large numbers of random matrices of this type.

Other Lefkovitch matrices: [generate_mpm_set\(\)](#)

Examples

```
set.seed(42) # set seed for repeatability

random_mpm(n_stages = 2, fecundity = 20, archetype = 1, split = FALSE)
random_mpm(n_stages = 2, fecundity = 20, archetype = 2, split = TRUE)
```

```
random_mpm(n_stages = 3, fecundity = 20, archetype = 3, split = FALSE)
random_mpm(n_stages = 4, fecundity = 20, archetype = 4, split = TRUE)
random_mpm(
  n_stages = 5, fecundity = c(0, 0, 4, 8, 10), archetype = 4,
  split = TRUE
)
# Using a range of values for fecundity
random_mpm(n_stages = 2, fecundity = 20, archetype = 1, split = TRUE)
```

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