## Package 'sketching'

October 14, 2022

Lee, S. and Ng, S. (2022). "Least Squares Estimation Using Sketched Data with Heteroskedas-

```
tic Errors," Proceedings of the 39th International Conference on Machine Learn-
     ing (ICML22), 162:12498-12520.
     Lee, S. and Ng, S. (2020). "An Econometric Perspective on Algorithmic Subsampling," An-
     nual Review of Economics, 12(1): 45-80.
License GPL-3
Encoding UTF-8
LazyData true
RoxygenNote 7.2.0
Imports stats, MASS, Rcpp (>= 1.0.7), phangorn (>= 2.8.1)
LinkingTo Rcpp
Suggests knitr, rmarkdown, testthat (>= 3.0.0), lmtest (>= 0.9), ivreg
     (>= 0.6), sandwich (>= 3.0)
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Depends R (>= 4.1.0)
URL https://github.com/sokbae/sketching/
BugReports https://github.com/sokbae/sketching/issues
Config/testthat/edition 3
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```

Title Sketching of Data via Random Subspace Embeddings

For more details, see the following papers.

**Description** Construct sketches of data via random subspace embeddings.

Type Package

Version 0.1.2

AK

## **R** topics documented:

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## **Description**

Angrist-Krueger (AK) dataset is a data extract from US Censuses that was analyzed in Angrist and Krueger (1991). In particular, the current dataset is from the 1970 Census, consisting of men born 1920-1929 (Year 1929 is the omitted cohort group).

## Usage

ΑK

#### **Format**

A data frame with 247,199 rows and 42 variables:

LWKLYWGE Outcome: log weekly wages
EDUC Covariate of interest: years of education
YR20 Indicator variable for the year of birth: equals 1 if yob = 1920
YR21 Indicator variable for the year of birth: equals 1 if yob = 1921
YR22 Indicator variable for the year of birth: equals 1 if yob = 1922

YR23 Indicator variable for the year of birth: equals 1 if yob = 1923YR24 Indicator variable for the year of birth: equals 1 if yob = 1924

YR25 Indicator variable for the year of birth: equals 1 if yob = 1925

VR26 Indicator variable for the year of birth: equals 1 if yob = 1926

**YR26** Indicator variable for the year of birth: equals 1 if yob = 1926

**YR27** Indicator variable for the year of birth: equals 1 if yob = 1927

**YR28** Indicator variable for the year of birth: equals 1 if yob = 1928

QTR120 Quarter-of-birth indicator interacted with year-of-birth indicator

QTR121 Quarter-of-birth indicator interacted with year-of-birth indicator

QTR122 Quarter-of-birth indicator interacted with year-of-birth indicator

QTR123 Quarter-of-birth indicator interacted with year-of-birth indicator

QTR124 Quarter-of-birth indicator interacted with year-of-birth indicator

QTR125 Quarter-of-birth indicator interacted with year-of-birth indicator

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QTR126 Quarter-of-birth indicator interacted with year-of-birth indicator QTR127 Quarter-of-birth indicator interacted with year-of-birth indicator QTR128 Quarter-of-birth indicator interacted with year-of-birth indicator QTR129 Quarter-of-birth indicator interacted with year-of-birth indicator QTR220 Quarter-of-birth indicator interacted with year-of-birth indicator QTR221 Quarter-of-birth indicator interacted with year-of-birth indicator QTR222 Quarter-of-birth indicator interacted with year-of-birth indicator QTR223 Quarter-of-birth indicator interacted with year-of-birth indicator QTR224 Quarter-of-birth indicator interacted with year-of-birth indicator QTR225 Quarter-of-birth indicator interacted with year-of-birth indicator QTR226 Quarter-of-birth indicator interacted with year-of-birth indicator QTR227 Quarter-of-birth indicator interacted with year-of-birth indicator QTR228 Quarter-of-birth indicator interacted with year-of-birth indicator QTR229 Quarter-of-birth indicator interacted with year-of-birth indicator QTR320 Quarter-of-birth indicator interacted with year-of-birth indicator QTR321 Quarter-of-birth indicator interacted with year-of-birth indicator QTR322 Quarter-of-birth indicator interacted with year-of-birth indicator QTR323 Quarter-of-birth indicator interacted with year-of-birth indicator QTR324 Quarter-of-birth indicator interacted with year-of-birth indicator QTR325 Quarter-of-birth indicator interacted with year-of-birth indicator QTR326 Quarter-of-birth indicator interacted with year-of-birth indicator QTR327 Quarter-of-birth indicator interacted with year-of-birth indicator QTR328 Quarter-of-birth indicator interacted with year-of-birth indicator QTR329 Quarter-of-birth indicator interacted with year-of-birth indicator CNST Constant

#### Source

The dataset is publicly available on Joshua Angrist's website at https://economics.mit.edu/faculty/angrist/data1/data/angkru1991/.

#### References

Angrist, J.D. and Krueger, A.B., 1991. Does compulsory school attendance affect schooling and earnings? Quarterly Journal of Economics, 106(4), pp.979–1014. doi:10.2307/2937954

4 simulation\_dgp

simulation_dgp Simulating observations from the data-generating process considere in Lee and $Ng$ (2022)	red
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## Description

Simulates observations from the data-generating process considered in Lee and Ng (2022)

## Usage

```
simulation_dgp(n, d, hetero = FALSE)
```

## **Arguments**

n sample size

d dimension of regressors from a multivariate normal distribution

hetero TRUE if the conditional variance of the error term is heteroskedastic and FALSE

if it is homoskedastic (default: FALSE)

## Value

An S3 object has the following elements.

Y n observations of outcomes
X n times d matrix of regressors

beta d dimensional vector of coefficients

### References

Lee, S. and Ng, S. (2022). "Least Squares Estimation Using Sketched Data with Heteroskedastic Errors," arXiv:2007.07781.

## **Examples**

```
data <- simulation_dgp(100, 5, hetero = TRUE) y <- dataY x <- dataX model <- lm(y ~ x)
```

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sketch Sketch

#### **Description**

Provides a subsample of data using sketches

#### Usage

```
sketch(data, m, method = "unif")
```

## **Arguments**

data (n times d)-dimensional matrix of data.

m (expected) subsample size that is less than n

method method for sketching: "unif" uniform sampling with replacement (default); "unif\_without\_replacement" uniform sampling without replacement; "bernoulli" Bernoulli sampling; "gaus-

uniform sampling without replacement; "bernoulli" Bernoulli sampling; "gaussian" Gaussian projection; "countsketch" CountSketch; "srht" subsampled randomized Hadamard transform; "fft" subsampled randomized trigonometric trans-

forms using the real part of fast discrete Fourier transform (stats::ftt).

#### Value

(m times d)-dimensional matrix of data For Bernoulli sampling, the number of rows is not necessarily m.

#### **Examples**

```
## Least squares: sketch and solve
# setup
n <- 1e+6 # full sample size
        # dimension of covariates
m <- 1e+3 # sketch size
# generate psuedo-data
X <- matrix(stats::rnorm(n*d), nrow = n, ncol = d)</pre>
beta \leftarrow matrix(rep(1,d), nrow = d, ncol = 1)
eps <- matrix(stats::rnorm(n), nrow = n, ncol = 1)</pre>
Y <- X %*% beta + eps
intercept \leftarrow matrix(rep(1,n), nrow = n, ncol = 1)
# full sample including the intercept term
fullsample <- cbind(Y,intercept,X)</pre>
# generate a sketch using CountSketch
s_cs <- sketch(fullsample, m, "countsketch")</pre>
# solve without the intercept
ls_cs \leftarrow lm(s_cs[,1] \sim s_cs[,2] - 1)
# generate a sketch using SRHT
s_srht <- sketch(fullsample, m, "srht")</pre>
# solve without the intercept
ls_srht <- lm(s_srht[,1] ~ s_srht[,2] - 1)</pre>
```

sketch\_leverage

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sketch	leverage

Sketch using leverage score type sampling

#### Description

Provides a subsample of data using sketches

#### Usage

```
sketch_leverage(data, m, method = "leverage")
```

## **Arguments**

data (n times d)-dimensional matrix of data. The first column needs to be a vector of

the dependent variable (Y)

m subsample size that is less than n

method method for sketching: "leverage" leverage score sampling using X (default);

"root\_leverage" square-root leverage score sampling using X.

#### Value

An S3 object has the following elements.

subsample (m times d)-dimensional matrix of data prob m-dimensional vector of probabilities

#### References

Ma, P., Zhang, X., Xing, X., Ma, J. and Mahoney, M. (2020). Asymptotic Analysis of Sampling Estimators for Randomized Numerical Linear Algebra Algorithms. Proceedings of the Twenty Third International Conference on Artificial Intelligence and Statistics, PMLR 108:1026-1035.

#### **Examples**

```
## Least squares: sketch and solve
# setup
n <- 1e+6 # full sample size
d <- 5  # dimension of covariates
m <- 1e+3 # sketch size
# generate psuedo-data
X <- matrix(stats::rnorm(n*d), nrow = n, ncol = d)
beta <- matrix(rep(1,d), nrow = d, ncol = 1)
eps <- matrix(stats::rnorm(n), nrow = n, ncol = 1)
Y <- X %*% beta + eps
intercept <- matrix(rep(1,n), nrow = n, ncol = 1)
# full sample including the intercept term</pre>
```

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```
fullsample <- cbind(Y,intercept,X)
# generate a sketch using leverage score sampling
s_lev <- sketch_leverage(fullsample, m, "leverage")
# solve without the intercept with weighting
ls_lev <- lm(s_lev$subsample[,1] ~ s_lev$subsample[,2] - 1, weights = s_lev$prob)</pre>
```

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