Package 'bizicount'

July 3, 2022

Title Bivariate Zero-Inflated Count Models Using Copulas

Version 1.1.0

Description Maximum likelihood estimation of copula-based zero-inflated
(and non-inflated) Poisson and negative binomial count models. Supports Frank
and Gaussian copulas. Allows for mixed margins (e.g., one margin Poisson, the
other zero-inflated negative binomial), and several marginal link functions.
Built-in methods for publication-quality tables using 'texreg', and post-estimation
diagnostics using 'DHARMa'. For information on copula regression for count data,
see Genest and Nešlehová (2007) <doi:10.1017/S0515036100014963> as well as
Nikoloulopoulos (2013) <doi:10.1007/978-3-642-35407-6_11>. For information on zero-inflated
count regression generally, see Lam-
bert (1992) <https:www.jstor.org/stable/1269547?origin=crossref>. The author
acknowledges support by NSF DMS-1925119 and DMS-212324.

License GPL (>= 3)

Encoding UTF-8

URL https://github.com/jmniehaus/bizicount

BugReports https://github.com/jmniehaus/bizicount/issues

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bizicount-package   *bizicount: Copula-Based Bivariate Zero-Inflated Count Regression Models*

Description

The package provides regression functions for copula-based bivariate count models, with and without zero-inflation, as well as regression functions for univariate zero-inflated count models. Generic methods from the [`texreg-package`](#) and [`DHARMa`](#) are extended to support this package, namely for the purposes of producing professional tables and carrying out post-estimation diagnostics.

Bivariate Functions

- [`bizicount`](#) – The primary function of this package. Carries out copula-based bivariate count regression via maximum likelihood using numerical optimization. Supports both zero-inflated and non-inflated distributions.

- [`extract.bizicount`](#) – Method for the texreg package's [`extract`](#) generic. Creates a list of texreg objects, one for each margin, for use with that package's other functions.

- [`make_DHARMa`](#) – Creates a list of DHARMa objects, one for each margin, for [`bizicount`](#) models. A wrapper around [`createDHARMa`](#).

- [`simulate.bizicount`](#) – Method that simulates observations using the fitted model's parameters, primarily for use with DHARMa.

Univariate Functions

- [`zic.reg`](#) – Univariate zero-inflated count regression models via maximum likelihood.

- [`extract.zicreg`](#) – Method for the texreg package's [`extract`](#) generic. Creates a texreg object that interfaces with that package's methods.

- [`simulate.zicreg`](#) – Method for simulating from the fitted model. Results are generally used for creating DHARMa objects.

Author(s)

John Niehaus

| bizicount | *Bizicount: Maximum likelihood estimation of copula-based bivariate zero-inflated (and non-inflated) count models* |

Description

The main bivariate regression function of the bizicount-package Estimates copula-based bivariate zero-inflated (and non-inflated) count models via maximum likelihood. Supports the Frank and Gaussian copulas, as well as zero-inflated Poisson and negative binomial margins (and their non-inflated counterparts). It's class has associated simulate methods for post-estimation diagnostics using the DHARMa package, as well as an extract method for printing professional tables using texreg. See the 'See Also' section for links to these methods.

Usage

```
bizicount(
  fmla1,
  fmla2,
  data,
  cop = "gaus",
  margins = c("pois", "pois"),
  link.ct = c("log", "log"),
  link.zi = c("logit", "logit"),
  scaling = "none",
  starts = NULL,
  keep = FALSE,
  subset,
  na.action,
  weights,
  frech.min = 1e-07,
  pmf.min = 1e-07,
  ...
)
```

Arguments

fmla1, fmla2	formulas for the first margin and second margins, respectively. If non-inflated, of the form y ~ x_1 + x_2 + ... + x_k; if inflated, of the form y ~ x1 + x2 + ... + x_k| z1 + z2 + ... + z_p, where y is the outcome for the first margin, x are covariates for count parameters, and z are covariates for zero-inflated parameters in each margin. All covariates can be the same.
data	A data.frame containing the response variables, covariates, and offsets for the model. If NULL, these quantities are searched for in the parent environment.

cop	Character string specifying the copula to be used. One of c("gaus", "frank"). Partial matching supported.
margins	Length 2 character vector specifying the marginal distributions for each outcome. Each of the two elements must be one of c("pois", "nbinom", "zip", "zinb"), and must be consistent with its corresponding formula (i.e., zero-inflated margins with zero-inflated formulas).
link.ct	Length 2 character string specifying the link function used for the count portion of each margin. One of c("log", "identity", "sqrt").
link.zi	Length 2 character string specifying the link function used for the zero-inflation portion of each margin. One of c("logit", "probit", "cauchit", "log", "cloglog"). Ignored if corresponding margins entry is not zero-inflated.
scaling	Character string (partial matching supported) indicating what type of scaling to apply to covariates (if any). One of c("none", "1sd", "gelman", "mm").

- "none" will apply no alterations to covariates.
- "1sd" will subtract off the mean, and divide by one standard deviation.
- "gelman" will subtract off the mean, and divide by two standard deviations, which makes binary and continuous variables have a similar interpretation. See Gelman (2008), "Scaling Regression Inputs by Dividing by Two Standard Deviations."
- "mm" will apply min-max normalization so that continuous covariates lie within a unit hypercube.

Factor variables, offsets, and the intercept are not scaled. If scaling, it is recommended that data be supplied in a dataframe (as opposed to from the global environment), otherwise the automated scaling cannot reliably be applied. The names of variables that have been scaled are returned as part of the bizicount object, in the list-element called scaled.

starts	Numeric vector of starting values for parameter estimates. See 'Details' section regarding the correct order for the values in this vector. If NULL, starting values are obtained automatically by a univariate regression fit.
keep	Logical indicating whether to keep the model matrix in the returned model object. Defaults to FALSE to conserve memory. NOTE: This must be set to TRUE to use the [texreg](), [simulate.bizicount](), [fitted](), or [make_DHARMa]() functions with bizicount objects.
subset	A vector indicating the subset of observations to use in estimation.
na.action	A function which indicates what should happen when the data contain NAs. Default is [na.omit]().
weights	An optional numeric vector of weights for each observation.
frech.min	Lower boundary for Frechet-Hoeffding bounds on copula CDF. Used for computational purposes to prevent over/underflow in likelihood search. Must be in $[0, 1e-5]$, with 0 imposing the original FH bounds without computational consideration. See 'Details.'
pmf.min	Lower boundary on copula PMF evaluations. Used for computational purposes to prevent over/underflow in likelihood search. Must be in $[0, 1e-5]$, with 0 imposing no bound. See 'Details.'
...	Additional arguments to be passed on to the quasi-newton fitting function, [nlm](). See 'Details' for some parameters that may be useful to alter.

Details

- `starts` – Starting values should be organized as follows:
    1. count parameters for margin 1
    2. count parameters for margin 2
    3. zero-inflated parameters for margin 1 (if applicable),
    4. zero-inflated parameters for margin 2 (if applicable),
    5. inverse dispersion parameter for margin 1 (if applicable),
    6. inverse dispersion parameter for margin 2 (if applicable)

  Thus, in general count parameters should come first, followed by zero-inflation parameters, and finally inverse dispersion parameters.

- `frech.min` – Changing this argument should almost never be necessary. Frechet (1951) and Hoeffding (1940) showed that copula CDFs have bounds of the form $max u + v - 1, 0 \leq C(u,v) \leq min u, v$, where u and v are uniform realizations derived from the probability integral transform. Due to numerical underflow, very small values of u and v can be rounded to zero. Particularly when evaluating the Gaussian copula CDF this is problematic, ultimately leading to infinite-valued likelihood evaluations. Therefore, we impose Frechet-Hoeffding bounds numerically as $max u + v - 1, frech.min \leq C(u,v) \leq min u, v, 1 - frech.min$. NOTE: Setting this to 0 imposes the original Frechet bounds mentioned above.

- `pmf.min` – Changing this argument should almost never be necessary. Observations can have likelihoods that are extremely close to 0. Numerically, these get rounded to 0 due to underflow. Then, taking logarithms results in an infinite likelihood. To avoid this, we bound PMF evaluations from below at `pmf.min`.

- `...` – Sometimes it may be useful to alter [nlm](#)'s default parameters. This can be done by simply passing those arguments into bizicount(). The two that seem to benefit the fitting process the most are `stepmax` and `steptol`. Readers are referred to the documentation on [nlm](#) for more details on these parameters. It can be useful to lower `stepmax` particularly when the Hessian is not negative definite at convergence, sometimes to a value between 0 and 1. It can also be beneficial to increase `steptol`.

Value

An S3 [bizicount-class](#) object, which is a list containing:

- `coef` – Coefficients of the model
- `coef.nid` – Coefficients without margin IDs
- `coef.orig` – Coefficients prior to transformations, for Gaussian dependence and negative binomial dispersion.
- `coef.orig.nid` – Coefficients prior to transforms, no margin IDs.
- `se` – Asymptotic normal-theory standard errors based on observed Fisher Information
- `se.nid` – Standard errors without margin IDs
- `z` – z-scores for parameter estimates
- `z.nid` – z-scores without margin IDs
- `p` – p-values for parameter estimates
- `p.nid` – p-values without margin IDs

- `coefmats` – A list containing coeficient matrices for each margin
- `loglik` – Scalar log-likelihood at convergence
- `grad` – Numerical gradient vector at convergence
- `n.iter` – Number of quasi-newton fitting iterations.
- `covmat` – Covariance matrix of parameter estimates based on observed Fisher Information
- `aic` – Model's Akaike information
- `bic` – Model's Bayesian information criterion
- `nobs` – Number of observations
- `margins` – Marginal distributions used in fitting
- `link.zi, link.ct` – Names of link functions used in fitting
- `invlink.ct, invlink.zi` – Inverse link functions used in fitting (the actual function, not their names)
- `outcomes` – Name of the response vector
- `conv` – Integer telling convergence status in nlm. See ?nlm.
- `cop` – The copula used in fitting
- `starts` – list of starting values used
- `call` – The model's call
- `model` – List containing model matrices, or `NULL` if keep = F.
- `scaled` – Vector indicating which covariates in each margin were scaled according to the `scaling` parameter.

Author(s)

John Niehaus

References

Genest C, Nešlehová J (2007). "A primer on copulas for count data." ASTIN Bulletin: The Journal of the IAA, 37(2), 475–515.

Inouye DI, Yang E, Allen GI, Ravikumar P (2017). "A review of multivariate distributions for count data derived from the Poisson distribution." Wiley Interdisciplinary Reviews: Computational Statistics, 9(3).

Joe H (1997). Multivariate models and multivariate dependence concepts. CRC Press.

Nikoloulopoulos A (2013). "Copula-Based Models for Multivariate Discrete Response Data." In P Jaworski, F Durante, WK Härdle (eds.), Copulae in Mathematical and Quantitative Finance, chapter 11, pp. 231–250. Springer.

Nelsen RB (2007). An Introduction to Copulas. Springer Science & Business Media.

Trivedi P, Zimmer D (2017). "A note on identification of bivariate copulas for discrete countdata." Econometrics, 5(1), 10.

Trivedi PK, Zimmer DM (2007). Copula modeling: an introduction for practitioners. NowPublishers Inc.

Examples

```
### bizicount example

## SETUP
set.seed(123)
n = 300

# define a function to simulate from a gaussian copula
# first margin is zero-inflated negative binomial (zinb)
# second margin is zero-inflated poisson (zip)
# Note: marginal distributions are hard-coded in function, including
# inverse dispersion parameter for zinb.
gen = function(n,
               b1,
               b2,
               g1,
               g2,
               dep) {

    k1 = length(b1)
    k2 = length(b2)

    X1 = cbind(1, matrix(rbinom(n * (k1 - 1), 1, .5), ncol = k1 - 1))
    X2 = cbind(1, matrix(rexp(n * (k2 - 1), 3), ncol = k2 - 1))

    lam1 = exp(X1 %*% b1)
    lam2 = exp(X2 %*% b2)

    Z1 = cbind(1, matrix(runif(n * (k1 - 1), -1, 1), ncol = k1 - 1))
    Z2 = cbind(1, matrix(rnorm(n * (k2 - 1)), ncol = k2 - 1))

    psi1 = plogis(Z1 %*% g1)
    psi2 = plogis(Z2 %*% g2)

    norm_vars = MASS::mvrnorm(
        n,
        mu = c(0, 0),
        Sigma = matrix(c(1, dep, dep, 1), ncol =2)
        )

    U = pnorm(norm_vars)

    y1 =  qzinb(U[, 1],
                mu = lam1,
               psi = psi1,
               size = .3)
    y2 =  qzip(U[, 2],
               lambda = lam2,
               psi = psi2)

    dat = data.frame(
        X1 = X1[, -1],
```

```
        X2 = X2[, -1],
        Z1 = Z1[, -1],
        Z2 = Z2[, -1],
        y1,
        y2,
        lam1,
        lam2,
        psi1,
        psi2
    )
    return(dat)
}


# define parameters
b1 = c(1, -2, 3)
b2 = c(-1, 3, 1)
g1 = c(2, -1.5, 2)
g2 = c(-1, -3.75, 1.25)
rho = .5


# generate data
dat = gen(n, b1, b2, g1, g2, rho)
f1 = y1 ~ X1.1 + X1.2 | Z1.1 + Z1.2
f2 = y2 ~ X2.1 + X2.2 | Z2.1 + Z2.2

## END SETUP

# estimate model

mod = bizicount(f1, f2, dat, cop = "g", margins = c("zinb", "zip"), keep=TRUE)

print(mod)
summary(mod)
```

---

bizicount-class   *The bizicount S4 Class*

Description

Note that `bizicount` objects are generally S3, and should use S3 syntax. This S4 class is defined only for compatability with [texreg](#). However, the contents of `bizicount` objects is the same in both S3 and S4, so the descriptions below apply in both cases.

Slots

`coef` Coefficients of the model

`coef.nid` Coefficients without margin IDs

coef.orig Coefficients prior to transformations, for Gaussian dependence and negative binomial dispersion.

coef.orig.nid Coefficients prior to transforms, no margin IDs.

se Asymptotic standard errors based on observed Fisher Information

se.nid Standard errors without margin IDs

z z-scores for parameter estimates

z.nid z-scores without margin IDs

p p-values for parameter estimates

p.nid p-values without margin IDs

coefmats A list containing coefficient matrices for each margin

loglik Scalar log-likelihood at convergence

grad Gradient vector at convergence

n.iter Number of quasi-newton fitting iterations.

covmat Covariance matrix of parameter estimates based on observed Fisher Information

aic Model's Akaike information

bic Model's Bayesian information criterion

nobs Number of observations

margins Marginal distributions used in fitting

link.zi,link.ct Names of link functions used in fitting

invlink.ct,invlink.zi Inverse link functions used in fitting (the actual function, not their names)

outcomes Name of the response vector

conv Integer telling convergence status.

cop The copula used in fitting

starts list of starting values used

call The model's call

model List containing model matrices, or NULL if keep = F.

scaled List indicating which covariates of each margin were scaled according to the scaling parameter.

---

extract.bizicount *Texreg for bizicount objects*

Description

This is a method for the [extract](#) generic to be used with objects that are output from the [bizicount](#) function. The results can be used with any of the [texreg-package](#) generics.

Usage

```
## S3 method for class 'bizicount'
extract(model, CI = NULL, id = TRUE)
```

Arguments

model	A `bizicount-class` model object (S3).
CI	The two-tailed confidence level, if confidence intervals are desired in the texreg object, otherwise `NULL`.
id	Logical indicating whether to prepend equation identifiers to coefficient names (`ct_` for count parameters, `zi_` for zero-inflated parameters)

Value

A `texreg-class` object, as produced by `createTexreg`, which can interface with all of that package's generics.

Note

Users can typically just call `texreg` directly on a `bizicount-class` object, instead of first extracting and then calling texreg.

Author(s)

John Niehaus

References

Leifeld, Philip (2013). texreg: Conversion of Statistical Model Output in R to LaTeX and HTML Tables. Journal of Statistical Software, 55(8), 1-24. URL http://dx.doi.org/10.18637/jss.v055.i08.

See Also

`extract`, `createTexreg`, `bizicount`

Examples

```
## SETUP
set.seed(123)
n = 500

# define a function to simulate from a gaussian copula
# first margin is zero-inflated negative binomial (zinb)
# second margin is zero-inflated poisson (zip)
# Note: marginal distributions are hard-coded in function, including
# inverse dispersion parameter for zinb.
gen = function(n,
               b1,
               b2,
               g1,
               g2,
               dep) {

    k1 = length(b1)
    k2 = length(b2)
```

```
        X1 = cbind(1, matrix(rbinom(n * (k1 - 1), 1, .5), ncol = k1 - 1))
        X2 = cbind(1, matrix(rexp(n * (k2 - 1), 3), ncol = k2 - 1))

        lam1 = exp(X1 %*% b1)
        lam2 = exp(X2 %*% b2)

        Z1 = cbind(1, matrix(runif(n * (k1 - 1), -1, 1), ncol = k1 - 1))
        Z2 = cbind(1, matrix(rnorm(n * (k2 - 1)), ncol = k2 - 1))

        psi1 = plogis(Z1 %*% g1)
        psi2 = plogis(Z2 %*% g2)

        norm_vars = MASS::mvrnorm(
            n,
            mu = c(0, 0),
            Sigma = matrix(c(1, dep, dep, 1), ncol =2)
        )

        U = pnorm(norm_vars)

        y1 =  qzinb(U[, 1],
                    mu = lam1,
                    psi = psi1,
                    size = .3)
        y2 =  qzip(U[, 2],
                    lambda = lam2,
                    psi = psi2)

        dat = data.frame(
            X1 = X1[, -1],
            X2 = X2[, -1],
            Z1 = Z1[, -1],
            Z2 = Z2[, -1],
            y1,
            y2,
            lam1,
            lam2,
            psi1,
            psi2
        )
        return(dat)
    }


    # define parameters
    b1 = c(1, -2, 3)
    b2 = c(-1, 3, 1)
    g1 = c(2, -1.5, 2)
    g2 = c(-1, -3.75, 1.25)
    rho = .5
```

```
# generate data
dat = gen(n, b1, b2, g1, g2, rho)
f1 = y1 ~ X1.1 + X1.2 | Z1.1 + Z1.2
f2 = y2 ~ X2.1 + X2.2 | Z2.1 + Z2.2

## END SETUP

# estimate model

mod = bizicount(f1, f2, dat, cop = "g", margins = c("zinb", "zip"), keep=TRUE)

# extract texreg objects, one with SEs, one with CIs
tr_obj_se = texreg::extract(mod)
tr_obj_ci = texreg::extract(mod, CI = .95)


# output to latex, single table.
# Note use of c(), because tr_obj_se, tr_obj_ci are lists.
texreg::texreg(c(tr_obj_se, tr_obj_ci))


# output as plaintext, two tables
texreg::screenreg(tr_obj_se)
texreg::screenreg(tr_obj_ci)
```

---

extract.zicreg   *Texreg for zicreg objects*

Description

This is a method for the `extract` generic to be used with objects that are output from the `zic.reg` function. The results can then interface with the `texreg-package`, as shown in examples below.

Usage

```
## S3 method for class 'zicreg'
extract(model, CI = NULL, id = TRUE)
```

Arguments

model	A zicreg model object, returned by `zic.reg`.
CI	The two-tailed confidence level, if desired in the resulting `texreg` object.
id	Logical indicating whether to prepend equation identifiers to coefficient names (`ct_` for count parameters, `zi_` for zero-inflated parameters)

Value

A `texreg-class` object, as produced by `createTexreg`, which can interface with all of that package's generics. See 'Examples.'

Author(s)

John Niehaus

References

Leifeld, Philip (2013). texreg: Conversion of Statistical Model Output in R to LaTeX and HTML
Tables. Journal of Statistical Software, 55(8), 1-24. URL http://dx.doi.org/10.18637/jss.v055.i08.

See Also

[extract](), [createTexreg](), [zic.reg]()

Examples

```
# Simulate some zip data
n=1000
x = cbind(1, rnorm(n))
z = cbind(1, rbeta(n, 4, 8))
b = c(1, 2.2)
g = c(-1, 1.7)
lam = exp(x %*% b)
psi = plogis(z %*% g)


y = bizicount::rzip(n, lambda = lam, psi=psi)
dat = cbind.data.frame(x = x[,-1], z = z[,-1], y = y)

# estimate model

mod = zic.reg(y ~ x | z, data = dat)


### Output to table with texreg

# extract information

tr_obj_se = texreg::extract(mod)
tr_obj_ci = texreg::extract(mod, CI = .95)

# output to latex, single table

texreg::texreg(list(tr_obj_se, tr_obj_ci))

# output to plain text, multiple tables

texreg::screenreg(tr_obj_se)
texreg::screenreg(tr_obj_ci)
```

---

make_DHARMa   *DHARMa-class objects from bizicount models*

Description

A wrapper around the DHARMa package's createDHARMa function. Creates a list of DHARMa objects, one for each margin of a bizicount-class object, using simulated responses from simulate.bizicount.

Usage

```
make_DHARMa(object, nsim = 250, seed = 123, method = "PIT")
```

Arguments

object	A bizicount-class object, as returned by bizicount.
nsim	Number of simulated responses from the fitted model to use for diagnostics.
seed	Random seed for simulating from fitted model.
method	See createDHARMa.

Value

A list of DHARMa objects.

Note

This is merely a wrapper around the createDHARMa function to conveniently get DHARMa objects for each margin of a bizicount model.

Author(s)

John Niehaus

References

Florian Hartig (2022). DHARMa: Residual Diagnostics for Hierarchical (Multi-Level / Mixed) Regression Models. R package version 0.4.5. https://CRAN.R-project.org/package=DHARMa

See Also

DHARMa, createDHARMa, simulate.bizicount

Examples

```
## SETUP
set.seed(123)
n = 150

# define a function to simulate from a gaussian copula
# first margin is zero-inflated negative binomial (zinb)
# second margin is zero-inflated poisson (zip)
# Note: marginal distributions are hard-coded in function, including
# inverse dispersion parameter for zinb.
gen = function(n, b1, b2, g1, g2, dep) {

    k1 = length(b1)
    k2 = length(b2)

    X1 = cbind(1, matrix(rbinom(n * (k1 - 1), 1, .5), ncol = k1 - 1))
    X2 = cbind(1, matrix(rexp(n * (k2 - 1), 3), ncol = k2 - 1))

    lam1 = exp(X1 %*% b1)
    lam2 = exp(X2 %*% b2)

    Z1 = cbind(1, matrix(runif(n * (k1 - 1), -1, 1), ncol = k1 - 1))
    Z2 = cbind(1, matrix(rnorm(n * (k2 - 1)), ncol = k2 - 1))

    psi1 = plogis(Z1 %*% g1)
    psi2 = plogis(Z2 %*% g2)

    norm_vars = MASS::mvrnorm(
        n,
        mu = c(0, 0),
        Sigma = matrix(c(1, dep, dep, 1), ncol =2)
    )

    U = pnorm(norm_vars)

    y1 =  qzinb(U[, 1],
                mu = lam1,
                psi = psi1,
                size = .3)
    y2 =  qzip(U[, 2],
               lambda = lam2,
               psi = psi2)

    dat = data.frame(
        X1 = X1[, -1],
        X2 = X2[, -1],
        Z1 = Z1[, -1],
        Z2 = Z2[, -1],
        y1,
        y2,
        lam1,
        lam2,
```

```
        psi1,
        psi2
    )
    return(dat)
}



# define parameters
b1 = c(1, -2, 3)
b2 = c(-1, 3, 1)
g1 = c(2, -1.5, 2)
g2 = c(-1, -3.75, 1.25)
rho = .5



# generate data
dat = gen(n, b1, b2, g1, g2, rho)
f1 = y1 ~ X1.1 + X1.2 | Z1.1 + Z1.2
f2 = y2 ~ X2.1 + X2.2 | Z2.1 + Z2.2

## END SETUP




# estimate model

mod = bizicount(f1, f2, dat, cop = "g", margins = c("zinb", "zip"), keep=TRUE)


# diagnose model with DHARMa
# see end for simulate.bizicount example.

dharm = make_DHARMa(mod, nsim = 150)

lapply(dharm, DHARMa::testResiduals)
```

---

predict.zicreg	*Predictions for univariate zero-inflated count regression models*

Description

Predicts the mean, probability, count mean, or zero-inflation probability for new data using parameters from a fitted zero-inflated count regression model.

Usage

```
## S3 method for class 'zicreg'
predict(object, newdata = NULL, y.new = NULL, type = "mean", ...)
```

Arguments

object	A fitted `zic.reg` object.
newdata	A `data.frame` containing new values of the same covariates appearing in fitted model.
y.new	An optional vector of new response values, used only for `type = "prob"`.
type	String, one of `c("mean", "prob", "psi", "lambda")`. `"mean"` will predict the conditional mean of the mixture distribution, `"prob"` will predict the probability of a new response value, `"psi"` will predict the probability of zero-inflation, and `"lambda"` will predict the mean of the count portion of the mixture distribution. NOTE: Setting `type = "mean"` and leaving `newdata = NULL` is the same as calling `fitted(object)`.
...	Ignored.

Value

A numeric vector containing the predictions using the model parameters.

Author(s)

John Niehaus

Examples

```
# Simulate some zip data
n=1000
x = cbind(1, rnorm(n))
z = cbind(1, rbeta(n, 4, 8))
b = c(1, 2.2)
g = c(-1, 1.7)
lam = exp(x %*% b)
psi = plogis(z %*% g)


y = bizicount::rzip(n, lambda = lam, psi=psi)
dat = cbind.data.frame(x = x[,-1], z = z[,-1], y = y)

# estimate model

mod = zic.reg(y ~ x | z, data = dat, keep = TRUE)


### Predict on observed/training data
# predict conditional mean (fitted values)
predict(mod, type = "mean")

# predict probabilty Y = y
probs_pred_obs = predict(mod, type = "prob")

# predict mean of count distribution (lambda)
lambda_pred_obs = predict(mod, type = "lambda")
```

```
# mse predicted vs true lambda values
mean((lam - lambda_pred_obs)**2)

# predict zero inflation probability (psi)
psi_pred_obs = predict(mod, type = "psi")

# MSE predicted vs true zero-inflation probabilities
mean((psi-psi_pred_obs)**2)


### Predict on test data
# simulate some test data

x = cbind(1, rnorm(n, mean = -0.5, sd = 1.25))
z = cbind(1, rbeta(n, 6, 12))
y = rzip(n, lambda = exp(x %*% coef(mod)[1:2]), psi = plogis(z %*% coef(mod)[3:4]))
dat_new = cbind.data.frame(x = x[,-1], z = z[,-1], y = y)

# predict conditional mean
mean_new = predict(mod, type = "mean", newdata = dat_new)
mean((y - mean_new)**2)

# predict probability of Y = y
probs_new = predict(mod, type = "prob", newdata = dat_new, y.new = y)

# predict lambda
lambda_new = predict(mod, type = "lambda", newdata = dat_new)

# predict zero inflation probability
psi_new = predict(mod, type = "psi", newdata = dat_new)
```

---

simulate.bizicount	*Simulating response values using parameters from fitted bizicount models*

Description

Simulates random response values using the fitted conditional mean function for each margin of a
[bizicount-class](#) object. Primarily for use with the [DHARMa](#) package.

Usage

```
## S3 method for class 'bizicount'
simulate(object, nsim = 250, seed = 123, ...)
```

Arguments

object	A fitted `bizicount-class` object, as returned by `bizicount`.
nsim	Number of simulated response values from the fitted model. E.g., `nsim = 250` will simulate each observation 250 times, for $n \times 250$ total observations.
seed	Seed used for simulating from fitted model. If `NULL`, no seed is set.
...	Ignored.

Value

A length 2 list, with each entry containing a numeric $nXnsim$ matrix for each margin of the bizicount model. Rows index the observation, and columns index the simulated dataset number.

Author(s)

John Niehaus

References

Florian Hartig (2022). DHARMa: Residual Diagnostics for Hierarchical (Multi-Level / Mixed) Regression Models. R package version 0.4.5. https://CRAN.R-project.org/package=DHARMa

See Also

`createDHARMa`, `simulateResiduals`

Examples

```
## SETUP
set.seed(123)
n = 150

# define a function to simulate from a gaussian copula
# first margin is zero-inflated negative binomial (zinb)
# second margin is zero-inflated poisson (zip)
# Note: marginal distributions are hard-coded in function, including
# inverse dispersion parameter for zinb.
gen = function(n,
               b1,
               b2,
               g1,
               g2,
               dep) {

    k1 = length(b1)
    k2 = length(b2)

    X1 = cbind(1, matrix(rbinom(n * (k1 - 1), 1, .5), ncol = k1 - 1))
    X2 = cbind(1, matrix(rexp(n * (k2 - 1), 3), ncol = k2 - 1))

    lam1 = exp(X1 %*% b1)
```

```
        lam2 = exp(X2 %*% b2)

        Z1 = cbind(1, matrix(runif(n * (k1 - 1), -1, 1), ncol = k1 - 1))
        Z2 = cbind(1, matrix(rnorm(n * (k2 - 1)), ncol = k2 - 1))

        psi1 = plogis(Z1 %*% g1)
        psi2 = plogis(Z2 %*% g2)

        norm_vars = MASS::mvrnorm(
            n,
            mu = c(0, 0),
            Sigma = matrix(c(1, dep, dep, 1), ncol =2)
        )

        U = pnorm(norm_vars)

        y1 =  qzinb(U[, 1],
                    mu = lam1,
                    psi = psi1,
                    size = .3)
        y2 =  qzip(U[, 2],
                   lambda = lam2,
                   psi = psi2)

        dat = data.frame(
            X1 = X1[, -1],
            X2 = X2[, -1],
            Z1 = Z1[, -1],
            Z2 = Z2[, -1],
            y1,
            y2,
            lam1,
            lam2,
            psi1,
            psi2
        )
        return(dat)
    }


    # define parameters
    b1 = c(1, -2, 3)
    b2 = c(-1, 3, 1)
    g1 = c(2, -1.5, 2)
    g2 = c(-1, -3.75, 1.25)
    rho = .5


    # generate data
    dat = gen(n, b1, b2, g1, g2, rho)
    f1 = y1 ~ X1.1 + X1.2 | Z1.1 + Z1.2
    f2 = y2 ~ X2.1 + X2.2 | Z2.1 + Z2.2
```

```
## END SETUP
```

```
# estimate model
mod = bizicount(f1, f2, dat, cop = "g", margins = c("zinb", "zip"), keep=TRUE)

# simulate from fitted model
sims = simulate(mod, nsim = 150)


# input sims to DHARMa for diagnostics
# margin 1
d1 = DHARMa::createDHARMa(
    simulatedResponse = sims[[1]],
    observedResponse = dat$y1,
    fittedPredictedResponse = fitted(mod)[,1],
    integerResponse = TRUE,
    method = "PIT"
)

# margin 2
d2 = DHARMa::createDHARMa(
    simulatedResponse = sims[[2]],
    observedResponse = dat$y2,
    fittedPredictedResponse = fitted(mod)[,2],
    integerResponse = TRUE,
    method = "PIT"
)

# test each margin
DHARMa::testResiduals(d1)
DHARMa::testResiduals(d2)
```

---

simulate.zicreg	*Simulating response values from fitted univariate zero-inflated count regression model*

Description

Simulates responses using the fitted parameters from a `zicreg-class` object, as returned by `zic.reg`. Primarily useful for methods found in `DHARMa` package. See 'Examples.'

Usage

```
## S3 method for class 'zicreg'
simulate(object, nsim = 250, seed = 123, ...)
```

Arguments

`object`	A `zicreg-class` model object, as returned by `zic.reg`.
`nsim`	Number of simulated datasets to create.
`seed`	Random seed for random number generation in simulations. If NULL, no seed is set.
`...`	Ignored.

Value

A numeric $n x nsim$ matrix, with rows indexing observations, and columns indexing the simulation number.

Author(s)

John Niehaus

References

Florian Hartig (2022). DHARMa: Residual Diagnostics for Hierarchical (Multi-Level / Mixed) Regression Models. R package version 0.4.5. https://CRAN.R-project.org/package=DHARMa

Examples

```
# Simulate some zip data
n=1000
x = cbind(1, rnorm(n))
z = cbind(1, rbeta(n, 4, 8))
b = c(1, 2.2)
g = c(-1, 1.7)
lam = exp(x %*% b)
psi = plogis(z %*% g)

y = bizicount::rzip(n, lambda = lam, psi=psi)
dat = cbind.data.frame(x = x[,-1], z = z[,-1], y = y)

# estimate model

mod = zic.reg(y ~ x | z, data = dat, keep = TRUE)

# simulate from fit for use in dharma
sims = simulate(mod)

### Make dharma object

dharm = DHARMa::createDHARMa(
    simulatedResponse = sims,
    observedResponse = y,
    fittedPredictedResponse = fitted(mod),
    integerResponse = TRUE,
    method = "PIT"
```

```
)

### Plot the DHARMa object, do other diagnostics
plot(dharm)
DHARMa::testResiduals(dharm)
```

---

zic.reg | *Univariate zero-inflated Poisson and negative binomial regression models*

Description

This function from the [bizicount](#) package estimates univariate zero-inflated Poisson and negative binomial regression models via maximum likelihood using either the [nlm](#) or [optim](#) optimization functions. It's class has associated [simulate](#) methods for post-estimation diagnostics using the [DHARMa](#) package, as well as an [extract](#) method for printing professional tables using [texreg](#). Visit the 'See Also' section for links to these methods for zicreg objects.

Usage

```
zic.reg(
  fmla = NULL,
  data,
  dist = "pois",
  link.ct = "log",
  link.zi = "logit",
  optimizer = "nlm",
  starts = NULL,
  subset,
  na.action,
  weights = rep(1, length(y)),
  X = NULL,
  z = NULL,
  y = NULL,
  offset.ct = NULL,
  offset.zi = NULL,
  warn.parent = T,
  keep = F,
  ...
)
```

Arguments

fmla
A [formula](#) of the form y ~ x_1 + x_2 + ... + x_n + offset(count_var) | z_1 + ... z_n + offset
where the x values are covariates in the count portion of the model, and z are
in the zero-inflation portion. The z and x variables can be the same. If NULL,
design matrices, the response vector, and offsets can be entered directly; see X,
z, y, offset.ct, and offset.zi below.

data   A [data.frame](#) containing all variables appearing in fmla, including offsets. If
                    not specified, variables are searched for in parent environment.

dist   The distribution used for the count portion of the zero-inflated mixture. One of
                    c("pois", "nbinom"), partial matching supported.

link.ct   String specifying the link function used for the count portion of the mixture
                    distribution. One of c("log", "identity", "sqrt"). See [family](#).

link.zi   Character string specifying the link function used for the zero-inflation por-
                    tion of the mixture distribution. One of c("logit", "probit", "cauchit",
                    "log", "cloglog"). See [family](#).

optimizer   String specifying the optimizer to be used for fitting, one of c("nlm", "optim").
                    If "optim", defaults to method="BFGS".

starts   Optional vector of starting values used for the numerical optimization procedure.
                    Should have count parameters first (with intercept first, if applicable), followed
                    by zero-inflated parameters (with intercept first, if applicable), and the inverse
                    dispersion parameter last (if applicable).

subset   Vector indicating the subset of observations on which to estimate the model

na.action   A function which indicates what should happen when the data contain NAs.
                    Default is [na.omit](#).

weights   An optional numeric vector of weights for each observation.

X, z   If fmla = NULL, these are the design matrices of covariates for the count and
                    zero-inflation portions, respectively. Both require no missingness. Similar in
                    spirit to [glm.fit](#) in that it can be faster for larger datasets because it bypasses
                    model matrix creation.

y   If fmla = NULL, a vector containing the response variable.

offset.ct, offset.zi
                    If fmla = NULL, vectors containing the (constant) offset for the count and zero-
                    inflated portions, respectively. Must be equal in length to y, and row-dim of X,
                    z. If left NULL, defaults to rep(0, length(y)).

warn.parent   Logical indicating whether to warn about data not being supplied.

keep   Logical indicating whether to keep the model matrices in the returned model
                    object. Must be TRUE to use [DHARMa](#) and [texreg](#) with the model object, e.g., via
                    [simulate.zicreg](#) and [extract.zicreg](#), as well as base generics like [fitted](#)
                    and [predict](#).

...   Additional arguments to pass on to the chosen optimizer, either [nlm](#) or [optim](#).
                    See 'Examples'.

Value

An S3 [zicreg-class](#) object, which is a list containing:

- call – The original function call
- obj – The class of the object
- coef – Vector of coefficients, with count, then zi, then dispersion.
- se – Vector of asymptotic standard errors

- `grad` – Gradient vector at convergence
- `link.ct` – Name of link used for count portion
- `link.zi` – Name of link used for zero-inflated portion
- `dist` – Name of distribution used for count portion
- `optimizer` – Name of optimization package used in fitting
- `coefmat.ct` – Coefficient matrix for count portion
- `coefmat.zi` – Coefficient matrix for zero-inflated portion
- `convergence` – Convergence code from optimization routine.
- `coefmat.all` – Coefficient matrix for both parts of the model
- `theta` – Coefficient matrix for dispersion, if applicable.
- `covmat` – Asymptotic covariance matrix
- `nobs` – Number of observations
- `aic` – Akaike information
- `bic` – Bayes information
- `loglik` – Log-likelihood at convergence
- `model` – List containing model matrices if keep = TRUE

Author(s)

John Niehaus

References

Lambert, Diane. "Zero-inflated Poisson regression, with an application to defects in manufacturing." Technometrics 34.1 (1992): 1-14.

See Also

[simulate.zicreg](), [extract.zicreg]()

Examples

```
## ZIP example
# Simulate some zip data
n=1000
x = cbind(1, rnorm(n))
z = cbind(1, rbeta(n, 4, 8))
b = c(1, 2.2)
g = c(-1, 1.7)
lam = exp(x %*% b)
psi = plogis(z %*% g)

y = bizicount::rzip(n, lambda = lam, psi=psi)
dat = cbind.data.frame(x = x[,-1], z = z[,-1], y = y)

# estimate zip model using NLM, no data.frame
```

```
mod = zic.reg(y ~ x[,-1] | z[,-1])

# same model, with dataframe

mod = zic.reg(y ~ x | z, data = dat)


# estimate zip using NLM, adjust stepmax via ... param

mod = zic.reg(y ~ x[,-1] | z[,-1], stepmax = .5)


# estimate zip using optim

mod = zic.reg(y ~ x[,-1] | z[,-1], optimizer = "optim")


# pass different method, reltol to optim using ... param

mod = zic.reg(y ~ x[,-1] | z[,-1],
        optimizer = "optim",
        method = "Nelder-Mead",
        control = list(reltol = 1e-10)
        )

# No formula, specify design matrices and offsets.
zic.reg(y=y, X=x, z=z)



## ZINB example
# simulate zinb data

disp = .5
y = bizicount::rzinb(n, psi = psi, size = disp, mu=lam)


# zinb model, use keep = TRUE for post-estimation methods

mod = zic.reg(y ~ x[,-1] | z[,-1], dist = "n", keep = TRUE)

print(mod)
summary(mod)
```

---

zicreg-class   *The zicreg S4 Class*

Description

Note that `zicreg` objects are, in general, S3. However, this S4 class is defined for compatability with `texreg`. Interaction with `zicreg` objects should generally use S3 syntax, but the below objects have the same name in both the S3 and S4 objects (but are in a list for S3).

Slots

`call` The original function call

`obj` The class of the object

`coef` Vector of coefficients, with count, then zi, then dispersion.

`se` Vector of asymptotic standard errors

`grad` Gradient vector at convergence

`link.ct` Name of link used for count portion

`link.zi` Name of link used for zero-inflated portion

`dist` Name of distribution used for count portion

`optimizer` Name of optimization package used in fitting

`coefmat.ct` Coefficient matrix for count portion

`coefmat.zi` Coefficient matrix for zero-inflated portion

`convergence` Convergence code from optimization routine.

`coefmat.all` Coefficient matrix for both parts of the model

`theta` Coefficient matrix for dispersion, if applicable.

`covmat` Asymptotic covariance matrix

`nobs` Number of observations

`aic` Akaike information

`bic` Bayes information

`loglik` Log-likelihood at convergence

`model` List containing model matrices if `keep = TRUE`

---

zinb   *The zero-inflated negative binomial (ZINB) distribution*

Description

These functions are used to evaluate the zero-inflated negative binomial distribution's probability mass function (PMF), cumulative distribution function (CDF), and quantile function (inverse CDF), as well as generate random realizations from the ZINB distribution.

Usage

```
dzinb(
  x,
  size,
  psi,
  mu = NULL,
  prob = NULL,
  lower.tail = TRUE,
  log = FALSE,
  recycle = FALSE
)

pzinb(
  q,
  size,
  psi,
  mu = NULL,
  prob = NULL,
  lower.tail = TRUE,
  log.p = FALSE,
  recycle = FALSE
)

qzinb(
  p,
  size,
  psi,
  mu = NULL,
  prob = NULL,
  lower.tail = TRUE,
  log.p = FALSE,
  recycle = FALSE
)

rzinb(n, size, psi, mu = NULL, prob = NULL, recycle = FALSE)
```

Arguments

x, q	Vector of quantiles at which to evaluate the PMF and CDF, respectively. Should be non-negative integers.
size	The inverse dispersion parameter, or number of successful trials, both for the negative binomial portion of the ZINB mixture distribution. See [nbinom]().
psi	Vector of zero-inflation probabilities.
mu	Vector of means for the count portion of the zero-inflated negative binomial distribution. Only one of mu or prob should be specified, not both. Should be non-negative. NOTE: This is *not* the mean of the ZINB distribution; it is the mean of the NB component of the mixture distribution. See [nbinom]().

prob	The probability of success on each trial in the negative binomial portion of the mixture distribution. Only one of mu or prob should be specified, not both. See [nbinom]().
lower.tail	Logical indicating whether probabilities should be $Pr(X \leq x)$ or $Pr(X > x)$
log, log.p	Logical indicating whether probabilities should be returned on log scale (for dzip and pzip), or are supplied on log-scale (for qzip).
recycle	Logical indicating whether to permit arbitrary recycling of arguments with unequal length. See 'Details' and 'Examples.'
p	Vector of probabilities at which to evaluate the quantile function.
n	Number of realizations to generate from the distribution

Value

dzinb returns the mass function evaluated at x, pzinb returns the CDF evaluated at q, qzinb returns the quantile function evaluated at p, and rzinb returns random realizations with the specified parameters.

Author(s)

John Niehaus

References

Lambert, Diane. "Zero-inflated Poisson regression, with an application to defects in manufacturing." Technometrics 34.1 (1992): 1-14.

Examples

```
# zero-inflated negative binomial examples

# two unique lengthed arguments, one is length 1 though. No error.

dzinb(4, size=.25, mu= c(1,2,3), psi=c(.2, .1, .15))


# two unique lengthed arguments, one of them is not length 1
# error
## Not run:

    dzinb(5, size=c(.25, .3), mu= c(1,2,3), psi=c(.2, .1, .15))


## End(Not run)


# two unique lengthed arguments, one of them is not length 1, set
# recycle = T, no error but can give innacurate results.

dzinb(5, size=c(.25, .3), mu= c(1,2,3), psi=c(.2, .1, .15), recycle=TRUE)
```

---

zip   *The zero-inflated Poisson (ZIP) distribution*

Description

These functions are used to evaluate the zero-inflated Poisson distribution's probability mass function (PMF), cumulative distribution function (CDF), and quantile function (inverse CDF), as well as generate random realizations from the ZIP distribution.

Usage

```
dzip(x, lambda, psi, log = FALSE, recycle = FALSE)

rzip(n, lambda, psi, recycle = FALSE)

pzip(q, lambda, psi, lower.tail = TRUE, log.p = FALSE, recycle = FALSE)

qzip(p, lambda, psi, lower.tail = TRUE, log.p = FALSE, recycle = FALSE)
```

Arguments

x, q	Vector of quantiles at which to evaluate the PMF and CDF, respectively. Should be non-negative integers.
lambda	Vector of means for the count portion of the zero-inflated Poisson distribution. Should be non-negative. NOTE: This is *not* the mean of the zero-inflated Poisson distribution; it is the mean of the Poisson component of the mixture distribution. See 'Details.'
psi	Vector of zero-inflation probabilities.
log, log.p	Logical indicating whether probabilities should be returned on log scale (for dzip and pzip), or are supplied on log-scale (for qzip).
recycle	Logical indicating whether to permit arbitrary recycling of arguments with unequal length. See 'Details' and 'Examples.'
n	Number of realizations from the distribution to generate
lower.tail	Logical indicating whether probabilities should be $Pr(X \leq x)$ or $Pr(X > x)$
p	Vector of probabilities at which to evaluate the quantile function.

Details

The zero inflated Poisson distribution is a mixture of a Poisson and a degenerate point-mass at 0. It has the form

$$\psi + (1 - \psi)(\lambda^x e^{-}\lambda)/x!$$

, with mean $(1 - \psi)\lambda$. Thus, the parameter lambda above is the mean of the Poisson distribution that forms part of the zero-inflated distribution, *not* the mean of the ZIP distribution.

recycle – If FALSE (default), all arguments must have identical length, there can be two unique lengths for the arguments, provided that one of those lengths is 1. For example, lambda = c(1,2,3) and psi=.5 is acceptable because there are two unique lengths, and one of them is length 1. However, lambda=c(1,2,3) and psi=c(.5,.2) would fail, as there are two distinct lengths, none of which is 1. If TRUE, no additional checks (beyond those in base R's functions) are made to ensure that the argument vectors have the same length.

Value

dzip returns the mass function evaluated at x, pzip returns the CDF evaluated at q, qzip returns the quantile function evaluated at p, and rzip returns random variates with the specified parameters.

Author(s)

John Niehaus

References

Lambert, Diane. "Zero-inflated Poisson regression, with an application to defects in manufacturing." Technometrics 34.1 (1992): 1-14.

Examples

```
# Unequal lengths, but one of them is length 1, others are same length (3).
# No error.

x = c(1,2,3)
lambda = c(3,4,5)
psi = .1

dzip(x, lambda, psi)


# unequal lengths, at least one of them is not length 1,
# error

## Not run:

x = c(1,2,3)
lambda = c(3,4)
psi = .1

dzip(x, lambda, psi)


## End(Not run)

# unequal lengths, at least one of them is not length 1.
# but set recycle = T to permit arbitrary recycling.

x = c(1,2,3)
lambda = c(3,4)
```

```
psi = .1

dzip(x, lambda, psi, recycle=TRUE)
```

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